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Solving Systems of Linear Inequalities

Objective

Graph the solution set of a system of linear inequalities



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Two or more inequalities considered together are called a **system of inequalities**. The **solution set of a system of inequalities** is the intersection of the solution sets of the individual inequalities.

To graph the solution set of a system of inequalities, first graph the solution set of each inequality. The solution set of an inequality is a half-plane.

The solution set of the system of inequalities is the region of the plane represented by the intersection of the two shaded half-planes.

Example 1

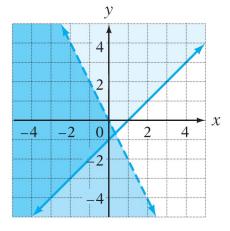
Graph the solution set.

$$\mathbf{A.} \quad y \ge x - 2x$$
$$y < -2x$$

A.
$$y \ge x - 1$$
 B. $2x + 3y > 9$ $y < -2x$ $y < -\frac{2}{3}x + 1$

Solution:





Shade above the solid line graph of

$$y = x - 1$$
.

Shade below the dashed line graph of

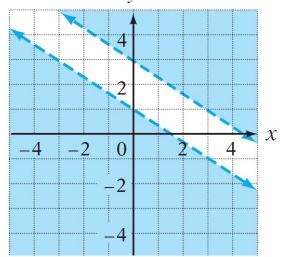
$$y = -2x$$
.

The solution set of the system is the intersection of the solution sets of the individual inequalities.

Example 1 – Solution

B.
$$2x + 3y > 9$$

 $3y > -2x + 9$
 $y > -\frac{2}{3}x + 3$



Solve
$$2x + 3y > 9$$
 for y.

Shade above the dashed line graph of $y = -\frac{2}{3}x + 3$.

Shade below the dashed line graph of $y = -\frac{2}{3}x + 1$.

The solution set of the system is the empty set because the solution sets of the two inequalities do not intersect.